



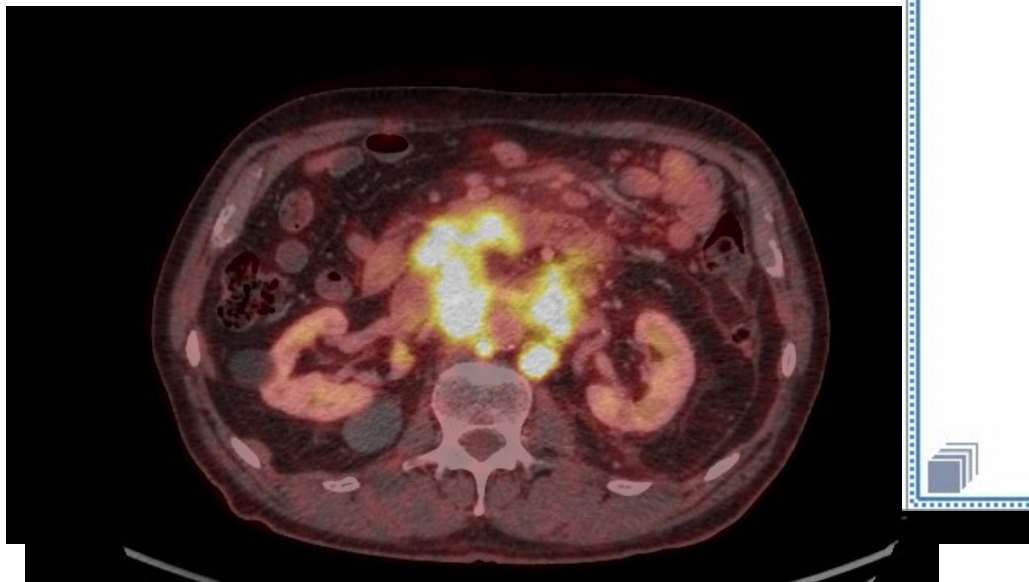
# Determination of glucose consumption, deoxyglucose method

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## [<sup>18</sup>F]FDG PET

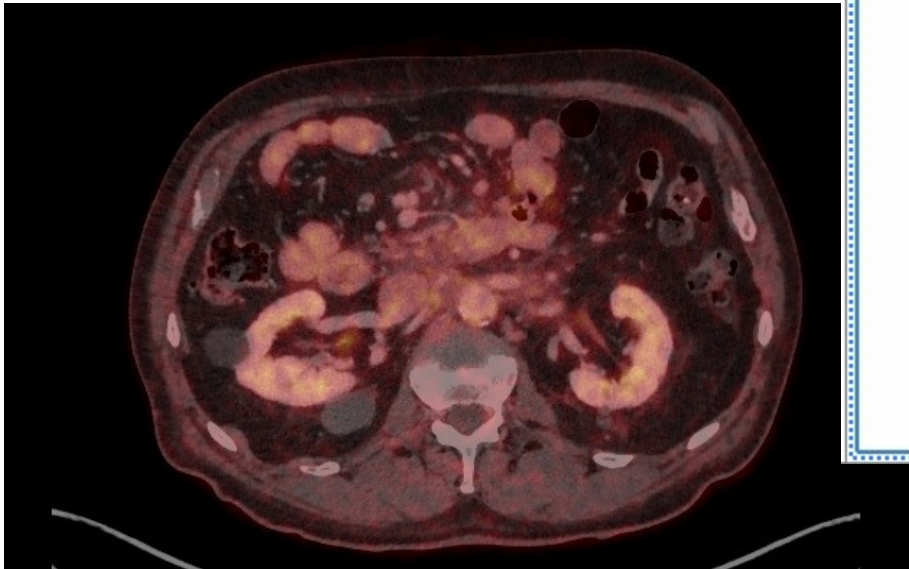
55 year-old-man with night sweats, and weight loss of 5 kg



## [<sup>18</sup>F]FDG PET

55 year-old-man with night sweats, and weight loss of 5 kg

Biopsy show lymphoma. After 6 cycles of chemotherapy this is his PET/CT scan:



## [<sup>18</sup>F]FDG PET

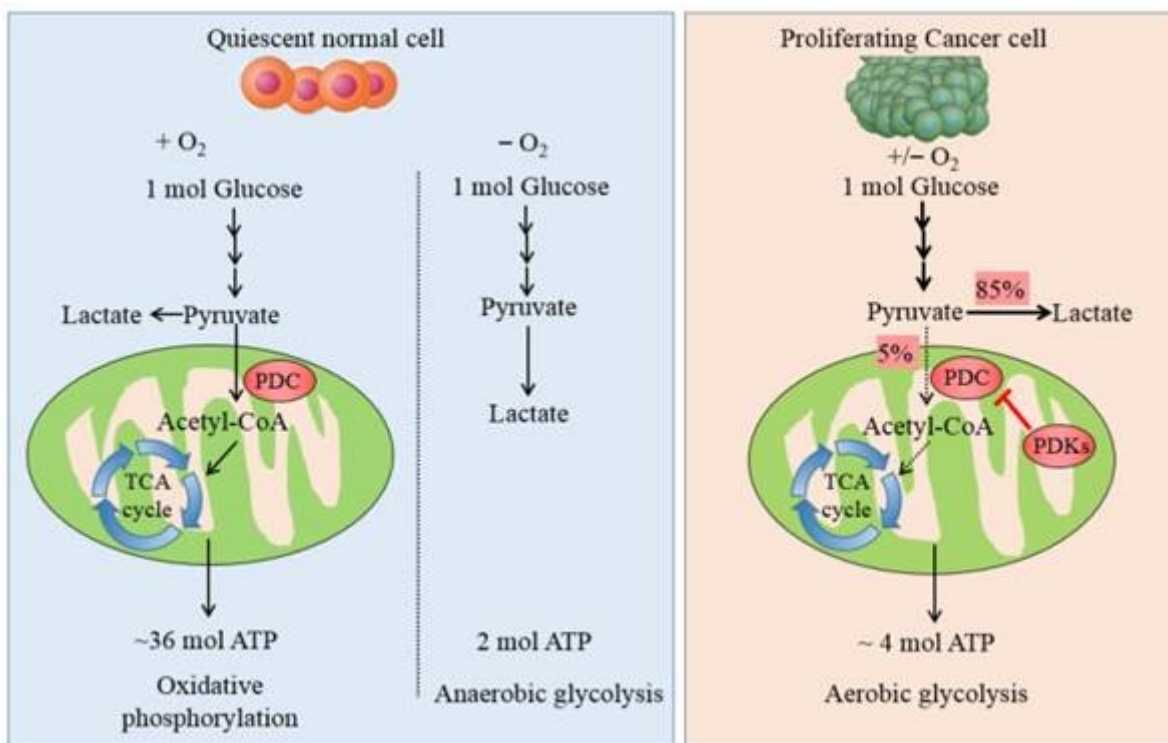
The introduction of [<sup>18</sup>F]FDG PET/CT has been a game changer in cancer diagnostics the last 25 years

But why is it so good?

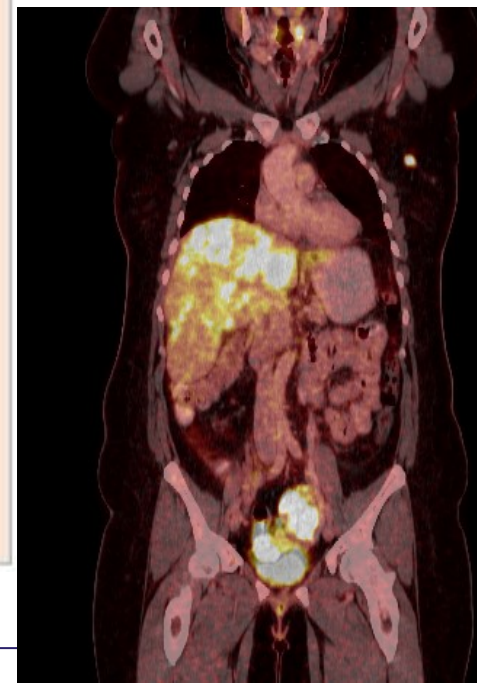


## The Warburg Effect

Cancer cells can change from oxidative phosphorylation to lactate production. Thereby glycolysis can be increased up to 200 times even at normal oxygen levels

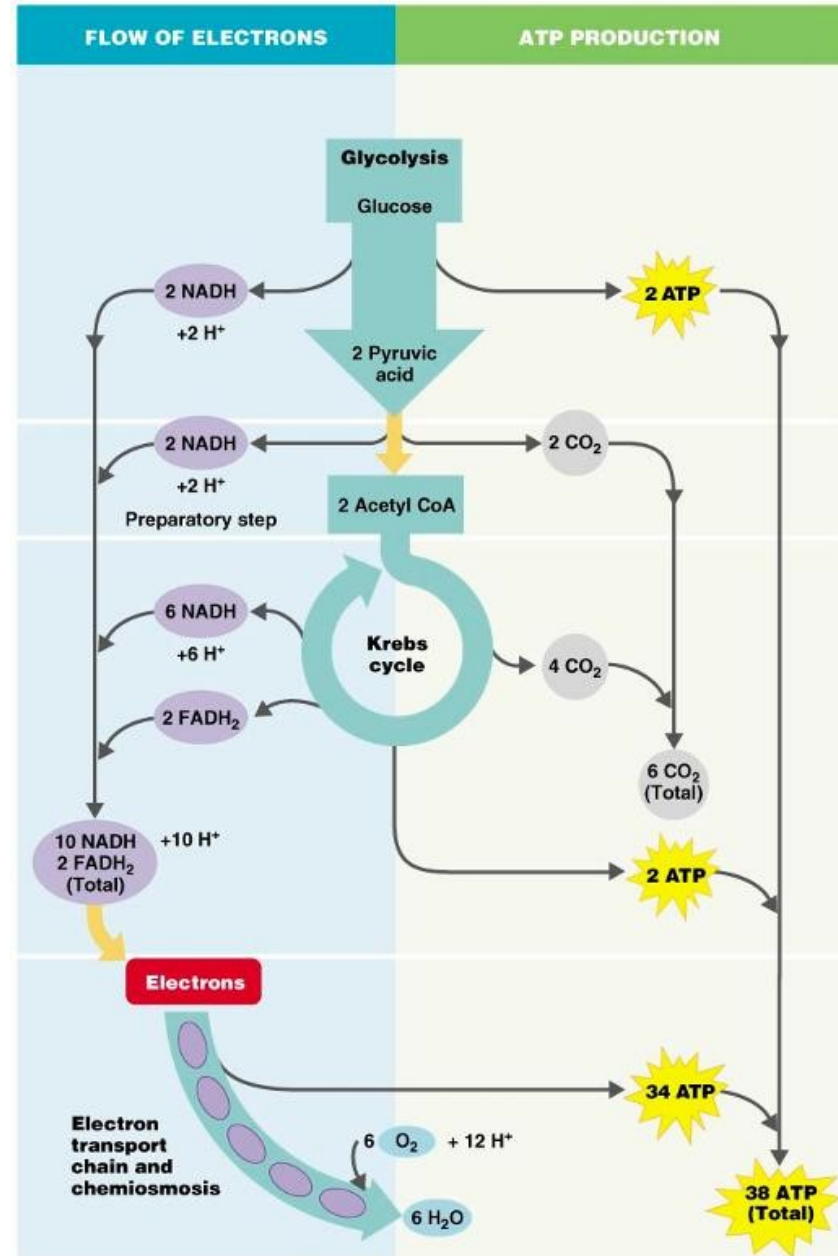


Otto H. Warburg  
1883 - 1970  
Nobel prize in physiology



## Glucose metabolism

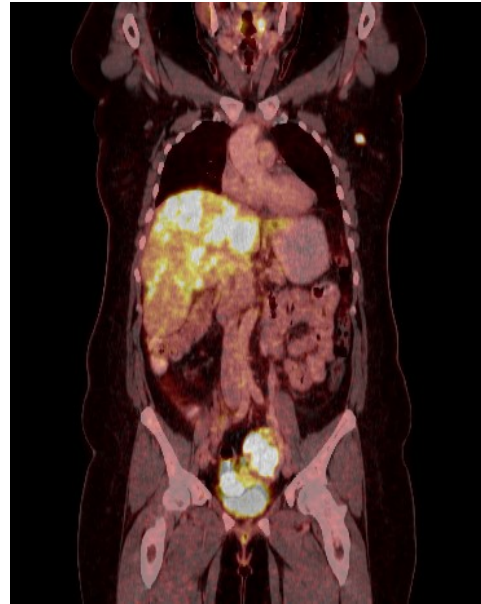
- Glycolysis requires no oxygen
- Only little energy production
- Oxygen consuming breakdown of glucose through Krebs cycle and electron chain reactions leads to high energy production
- Pyruvate can be transformed into lactate, which keeps NADH levels stable



## [<sup>18</sup>F]FDG PET

The introduction of [<sup>18</sup>F]FDG PET/CT has been a game changer in cancer diagnostics the last 25 years

Actually, [<sup>18</sup>F]FDG PET/CT is so good that you don't need to do quantification



Blobologi:

FDG PET/CT whole body imaging – hot spots correlate to quantitative  $K_i$  measures

## Thoracic Radiology

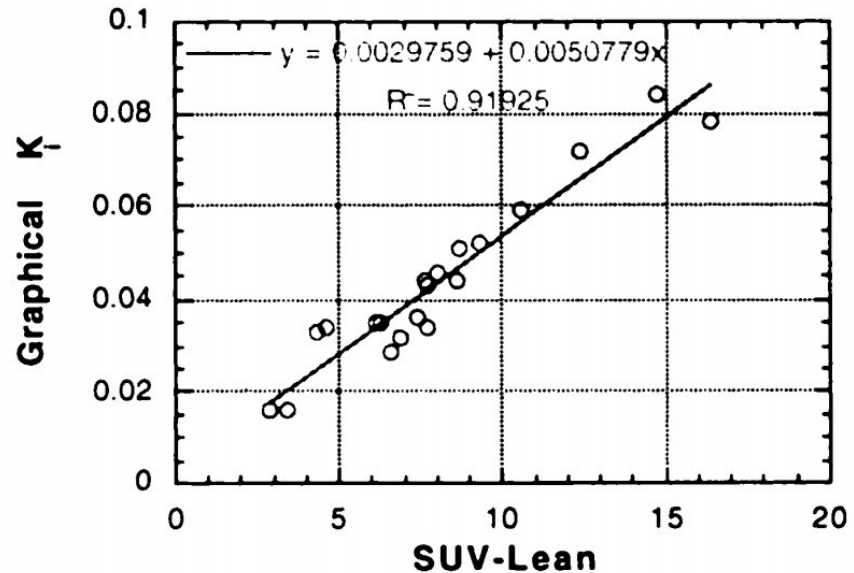
Heikki Minn, MD<sup>2</sup> • Kenneth R. Zasadny, PhD • Leslie E. Quint, MD • Richard L. Wahl, MD

### Lung Cancer: Reproducible Quantitative Measurements of 2-[F-18]-Fluoro-2-deoxy-D-glucose

**PURPOSE:** To study the precision of repeated 2-[fluorine-18]-fluoro-2-deoxy-D-glucose (FDG) uptake measurements at positron emission tomography (PET) in patients with primary lung cancer.

**MATERIALS AND METHODS:** Ten patients with untreated lung cancer

**POSITRON EMISSION TOMOGRAPHY (PET)** was used to measure FDG uptake in human tumors. The results represent oncologic ways re-



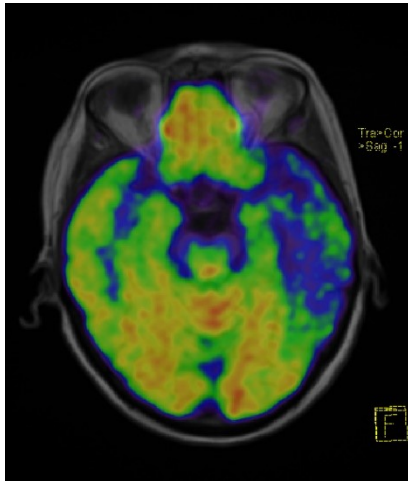
**Figure 5.** Relationship between SUV-lean and  $K_i$  in 20 FDG PET scans obtained in 10 patients with lung cancer.



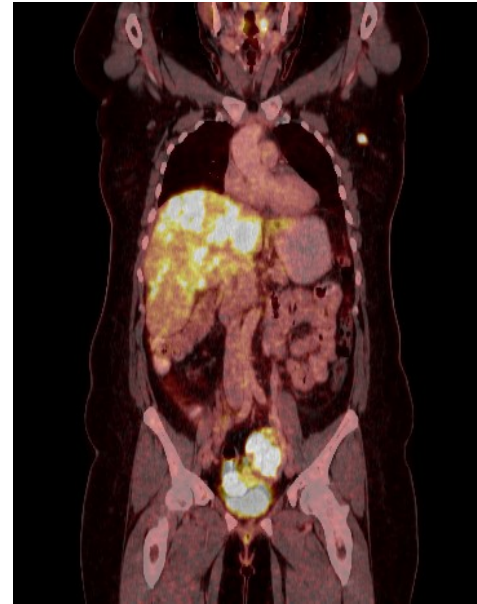
## [<sup>18</sup>F]FDG PET

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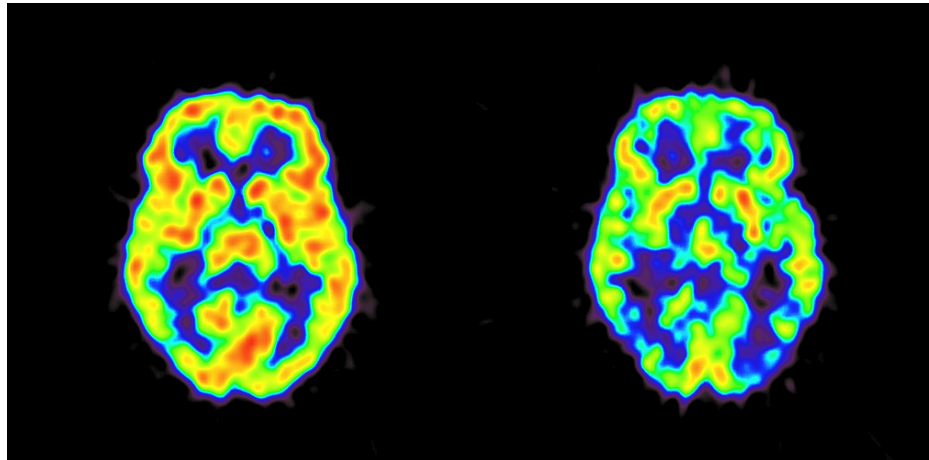


Temporal reduction in frontotemporal dementia (semantic dementia)



**No need for quantification when looking for regional differences or hotspots**

# Quantitation of regional metabolic rate of glucose - rMRglc



33% reduction in CMRglc  
during ketone infusion  
– **global changes**

## Glucose measurements methods

1. Global measurements
  - Using global blood flow measurements and Fick's principle
2. Regional measurements using imaging
  - Deoxyglucose method in animals
  - Fluoro-deoxyglucose method in humans



## THE FICK PRINCIPLE

“Everything that goes in and doesn't come out again has been taken up by the organ”

$$\text{Uptake} = F(C_a - C_v)$$

F= blood flow

$C_a$  and  $C_v$ = substrate concentrations in arterial and cerebral venous blood

F can be measured by the Fick Principle by using an inert gas (Xenon)



Disadvantages: Very invasive!

Catheter in the internal jugular vein is necessary to measure cerebral venous blood

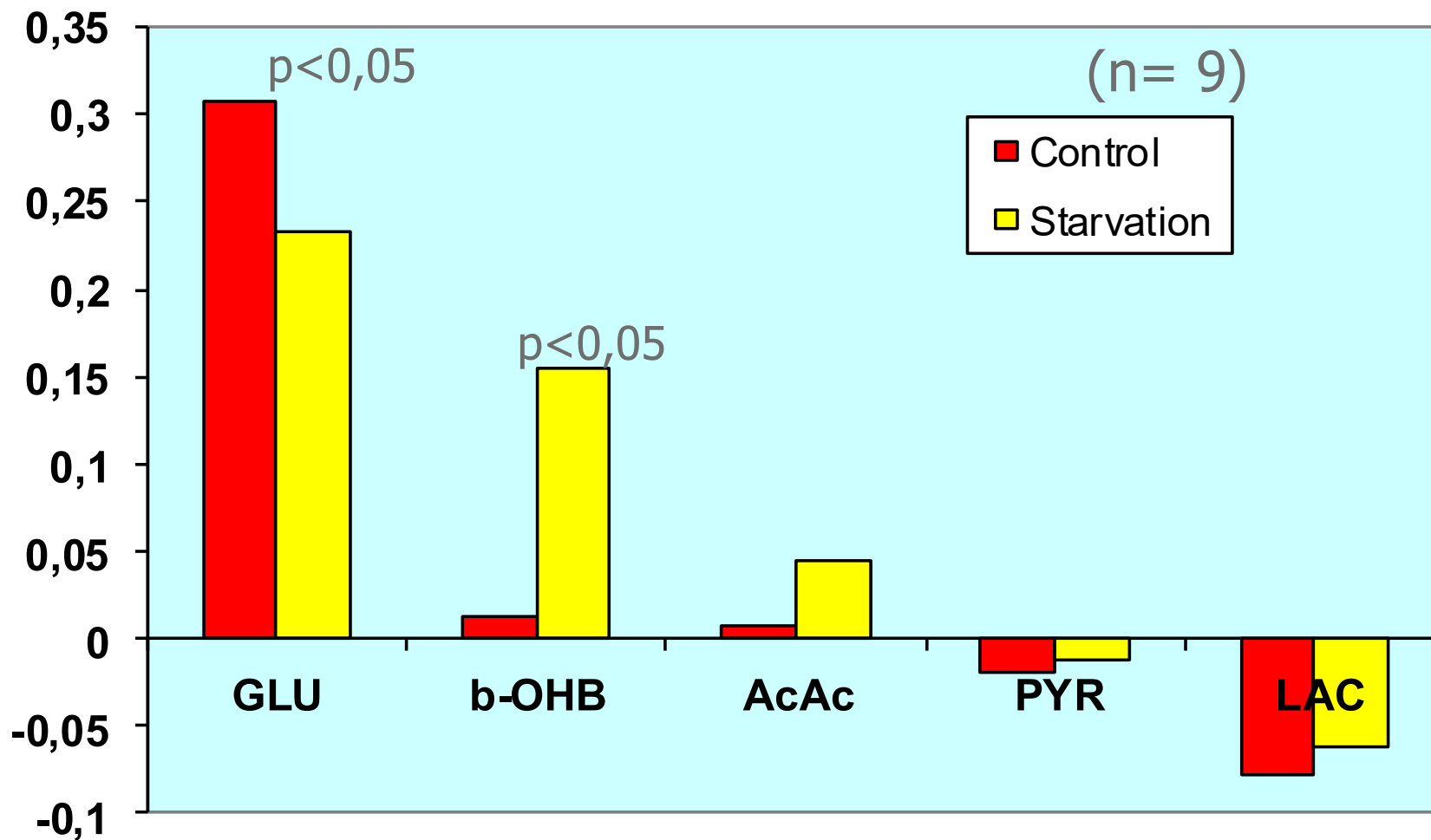


## Catheter in the internal jugular vein



Advantages: Almost everything can be measured  
Ex: Brain Carbohydrate Metabolism after 3.5 Days of Starvation

### Net Uptake (umol/g/min)



Hasselbalch et al., JCBF, 1994



# The deoxyglucose method

*Journal of Neurochemistry*, 1977, Vol. 28, pp. 897-916. Pergamon Press. Printed in Great Britain.

## THE [ $^{14}\text{C}$ ]DEOXYGLUCOSE METHOD FOR THE MEASUREMENT OF LOCAL CEREBRAL GLUCOSE UTILIZATION: THEORY, PROCEDURE, AND NORMAL VALUES IN THE CONSCIOUS AND ANESTHETIZED ALBINO RAT<sup>1</sup>

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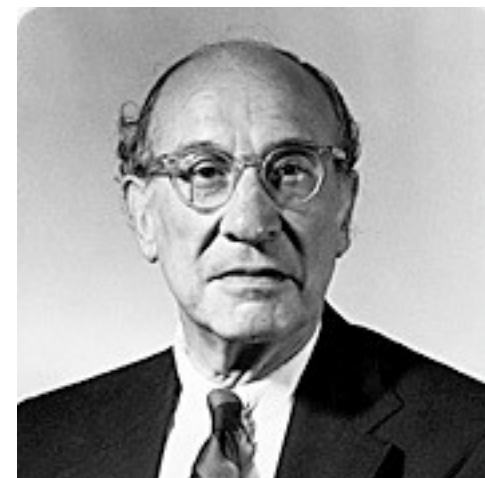
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(Received 3 November 1976. Accepted 12 January 1977)

**Abstract**—A method has been developed for the simultaneous measurement of the rates of glucose consumption in the various structural and functional components of the brain *in vivo*. The method can be applied to most laboratory animals in the conscious state. It is based on the use of 2-deoxy-D- [ $^{14}\text{C}$ ]glucose ([ $^{14}\text{C}$ ]DG) as a tracer for the exchange of glucose between plasma and brain and its phosphorylation by hexokinase in the tissues. [ $^{14}\text{C}$ ]DG is used because the label in its product,



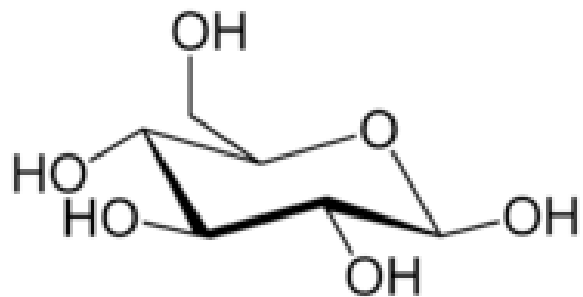
**Louis Sokoloff**

National Institute  
of Mental Health, NIH

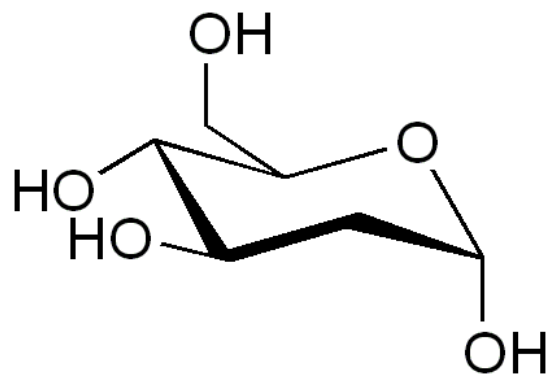
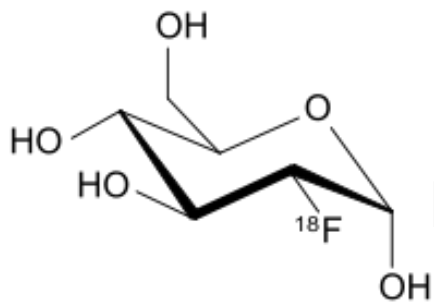
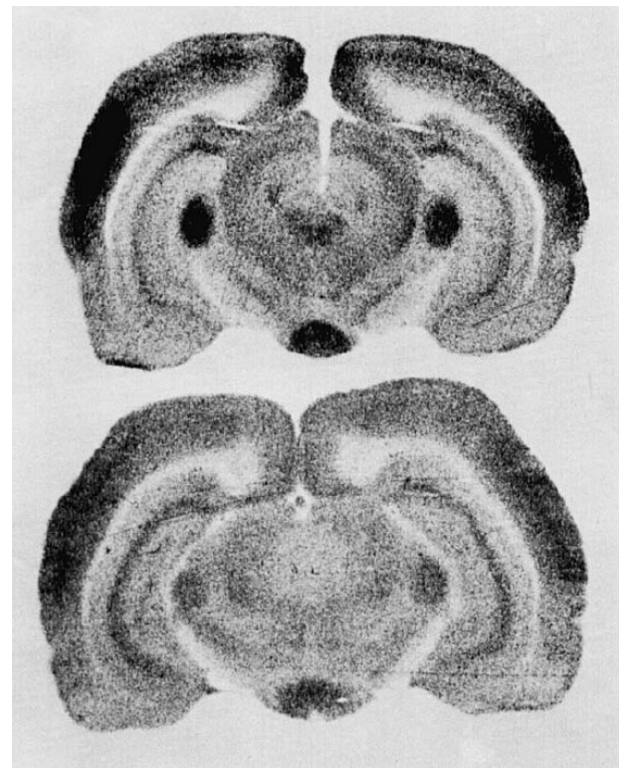




## The deoxyglucose method



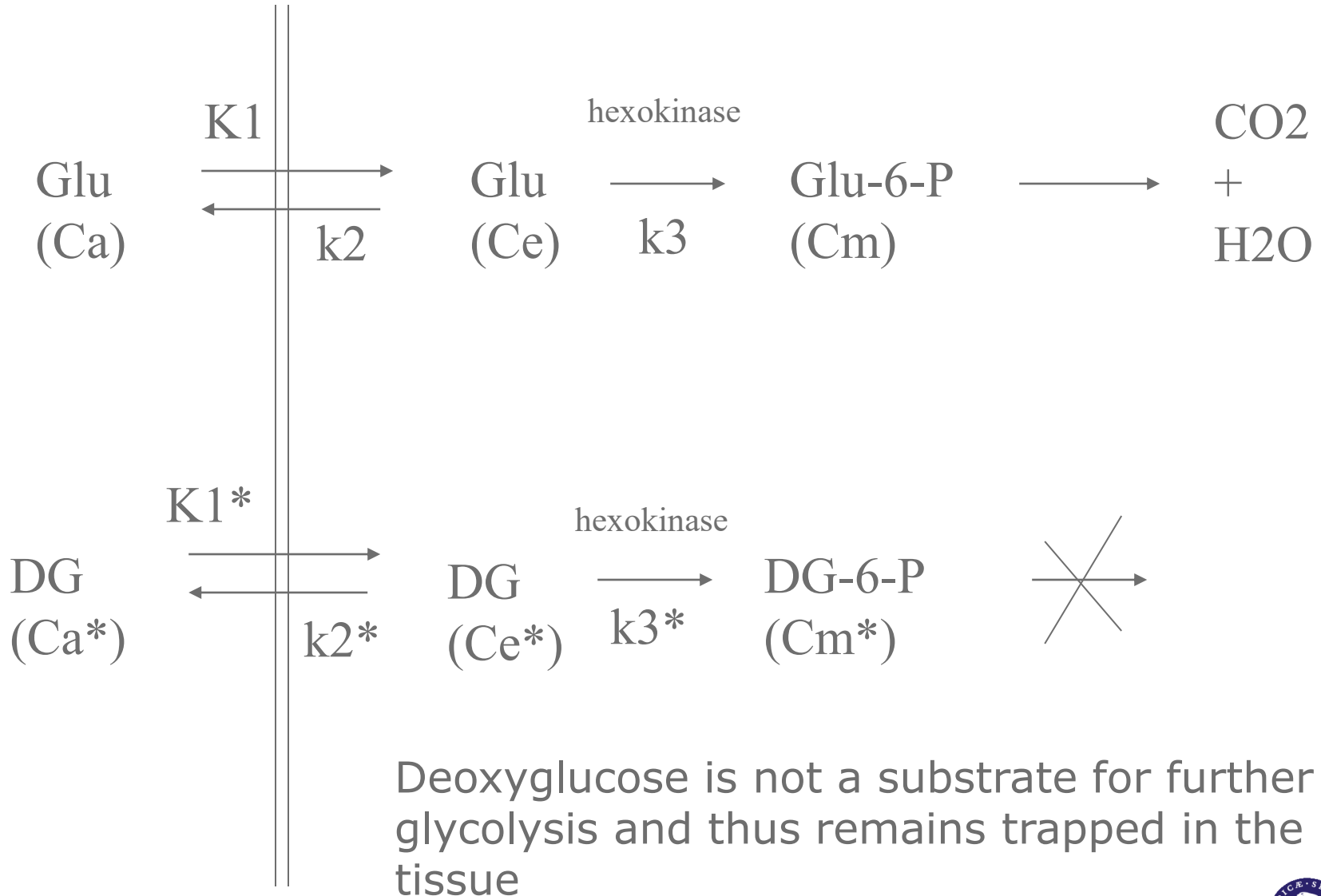
D-glucose

[<sup>14</sup>C]2-deoxy-D-glucose[<sup>18</sup>F]2-deoxy-D-glucose = [<sup>18</sup>F]FDG

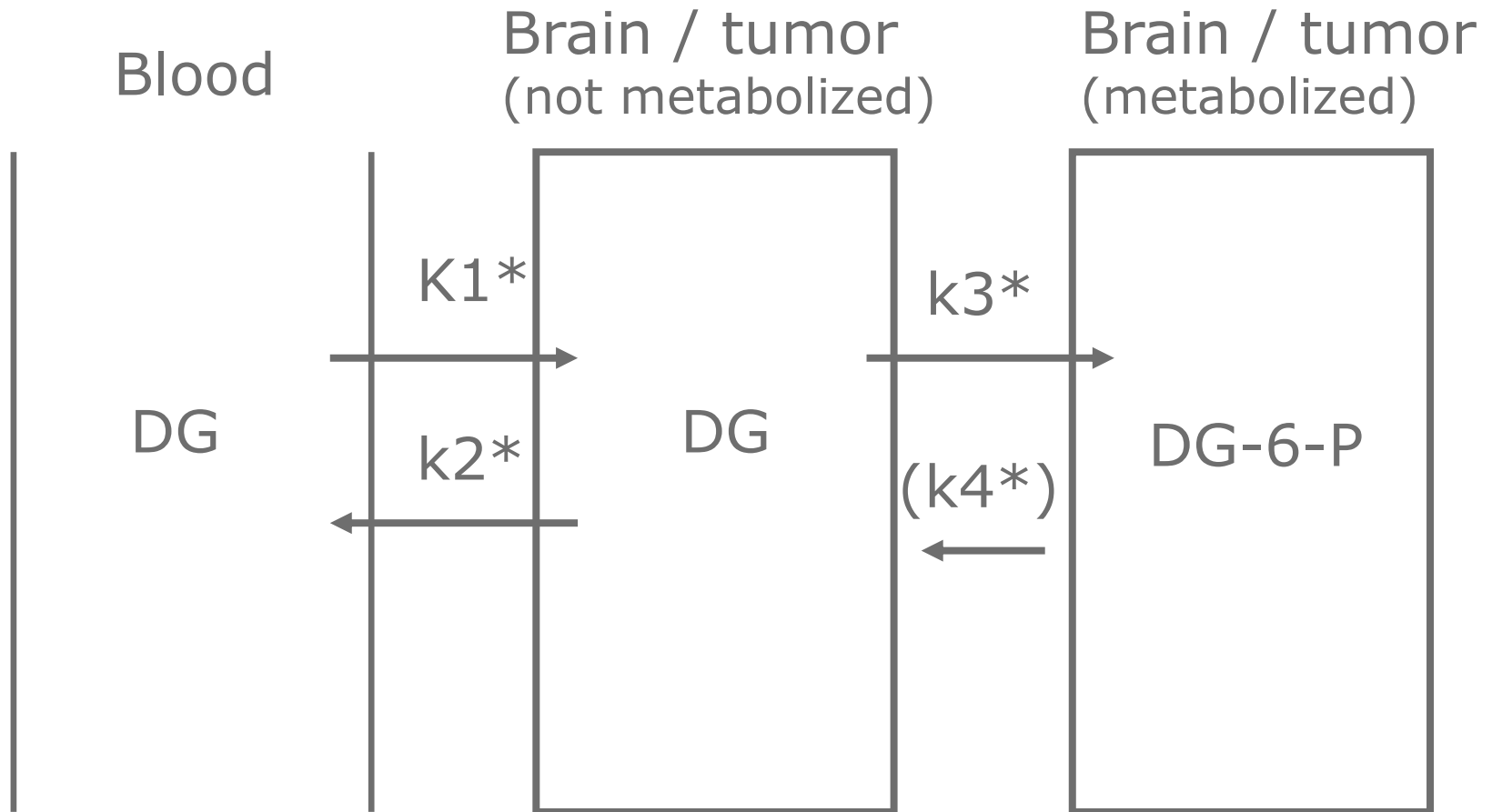
Blood

BBB

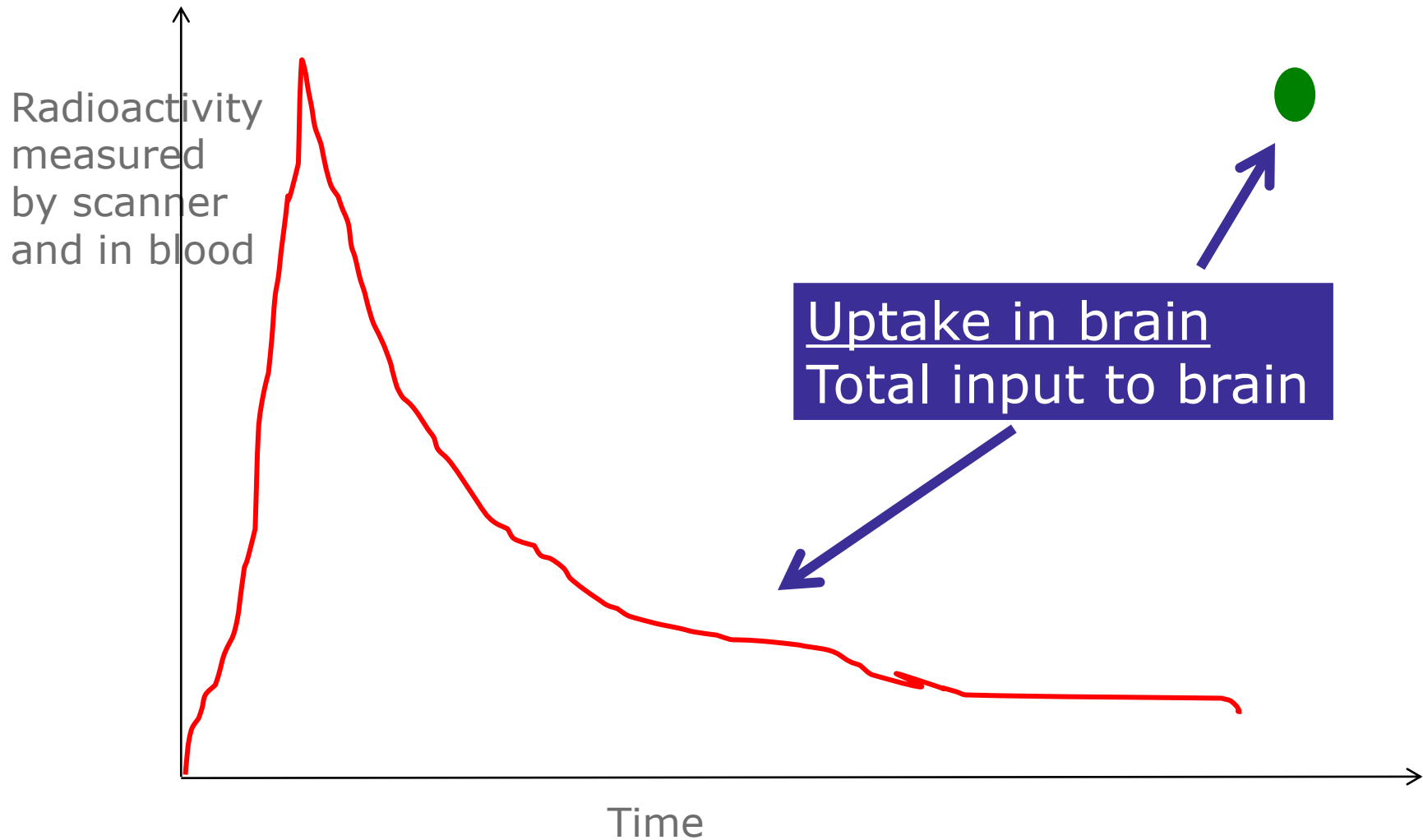
Brain / tumor



# Compartment model of Deoxy-Glucose metabolism



## CMRglc measured by 1 time point = “the autoradiographic method”



## The autoradiographic method - the Sokoloff equation

$^{14}\text{C}$ Deoxyglucose-phosphate formed  
between Time, 0 to T

Total  $^{14}\text{C}$  in  
Tissue at time, T

Tissue  $^{14}\text{C}$ deoxyglucose  
at time, T

subtracted by small  
correction terms

$R_i =$

$$R_i = \frac{C_i^*(T) - k_1^* e^{-(k_2^* + k_3^*)T} \int_0^T C_p^* e^{(k_2^* + k_3^*)t} dt}{\underbrace{[\lambda \cdot V_m^* \cdot K_m / \Phi \cdot V_m \cdot K_m^*]}_{\text{Lumped Constant}} \underbrace{\left[ \int_0^T (C_p^* / C_p) dt \right]}_{\text{Integrated Plasma Specific Activity}} - \underbrace{e^{-(k_2^* + k_3^*)T} \int_0^T (C_p^* / C_p) e^{(k_2^* + k_3^*)t} dt}_{\text{Correction for lag in Tissue Equilibration with plasma}}}$$

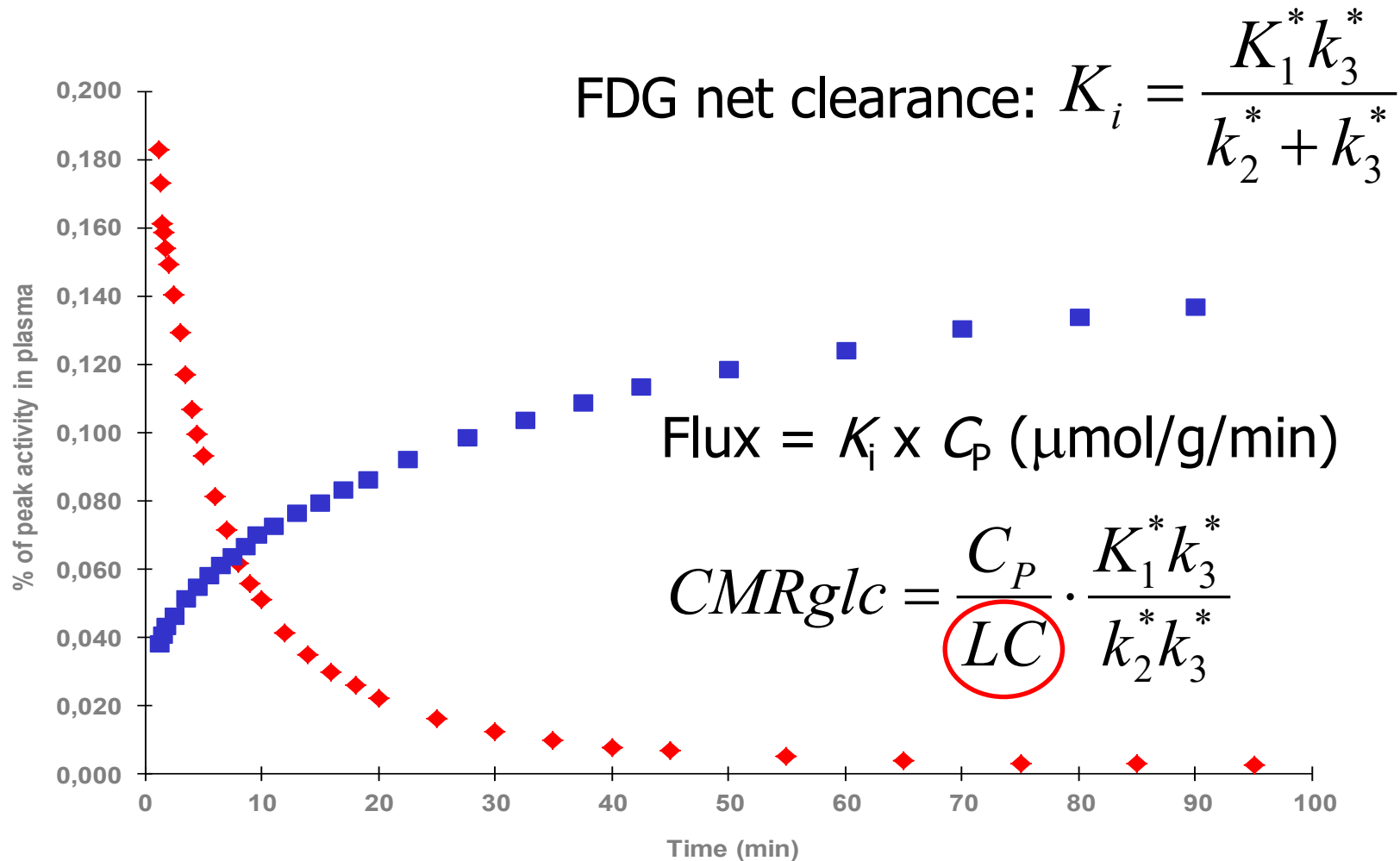
Integrated precursor specific activity in tissue

.. and corrected  
for difference  
between tracer  
and glucose itself

Sokoloff et al., 1977



# FDG uptake determined from compartment modeling ( $K_1^*$ - $k_3^*$ ) - "the dynamic method"



## Lumped Constant - LC

LC = Net Clearance of FDG / Net Clearance of Glucose

$$LC = \frac{K_i^*}{K_i} = \frac{\frac{K_1^* k_3^*}{k_2^* + k_3^*}}{\frac{K_1 k_3}{k_2 + k_3}} \quad K_i = \text{net clearance (mL/g/min)}$$

Hexokinase favors glucose over FDG, and transport favors FDG over glucose

Litterature values for LC for FDG in human brains: 0.65-0.81 Can change during hypoglycemia

In tumours the LC is highly variable and [<sup>18</sup>F]FDG PET may not allow accurate assessment of glucose utilization

Barrio et al. (2020) JNM :61(6)931-937



# Lumped Constant

## The FDG Lumped Constant in Normal

Humans are characterized by 6 constants. The formula for the LC, defined by Sokoloff et al., is:

Michael M. C  
Thomas K. L

<sup>1</sup>Division of Nu  
Department of  
University of H

$$LC = \frac{\lambda \cdot K_m \cdot V_{max}^*}{\phi \cdot V_{max} \cdot K_m^*} \quad \text{Eq. 1}$$

The lumped c  
glucose metab

**Methods:** LC  
male, 6 female  
pendently usi  
positron tomog  
gion-of-interes  
compartmenta  
mal brain was  
was slightly lo

**Conclusion:** T  
siderably high  
because of metabo  
study by Hasselbalch.

**Key Words:** FDG; <sup>11</sup>C-glucose; lumped constant; glucose metabolism

**J Nucl Med 2002; 43:1157–1166**

where  $\lambda$  is the ratio of the distribution volume of FDG to that of glucose,  $\phi$  is the fraction of glucose that continues down the Embden–Meyerhof pathway after being phosphorylated,  $K_m$  is the Michaelis–Menten constant for phosphorylation of glucose (\* indicates FDG), and  $V_{max}$  is the maximum velocity for phosphorylation of glucose (\* indicates FDG). The LC is used to convert  $MR_{FDG}$  to  $MR_{glc}$  by dividing  $MR_{FDG}$  by the LC. Clearly, the value of the LC is

critical in quantitative calculation of regional cerebral glucose metabolic rates when FDG is used as the tracer.

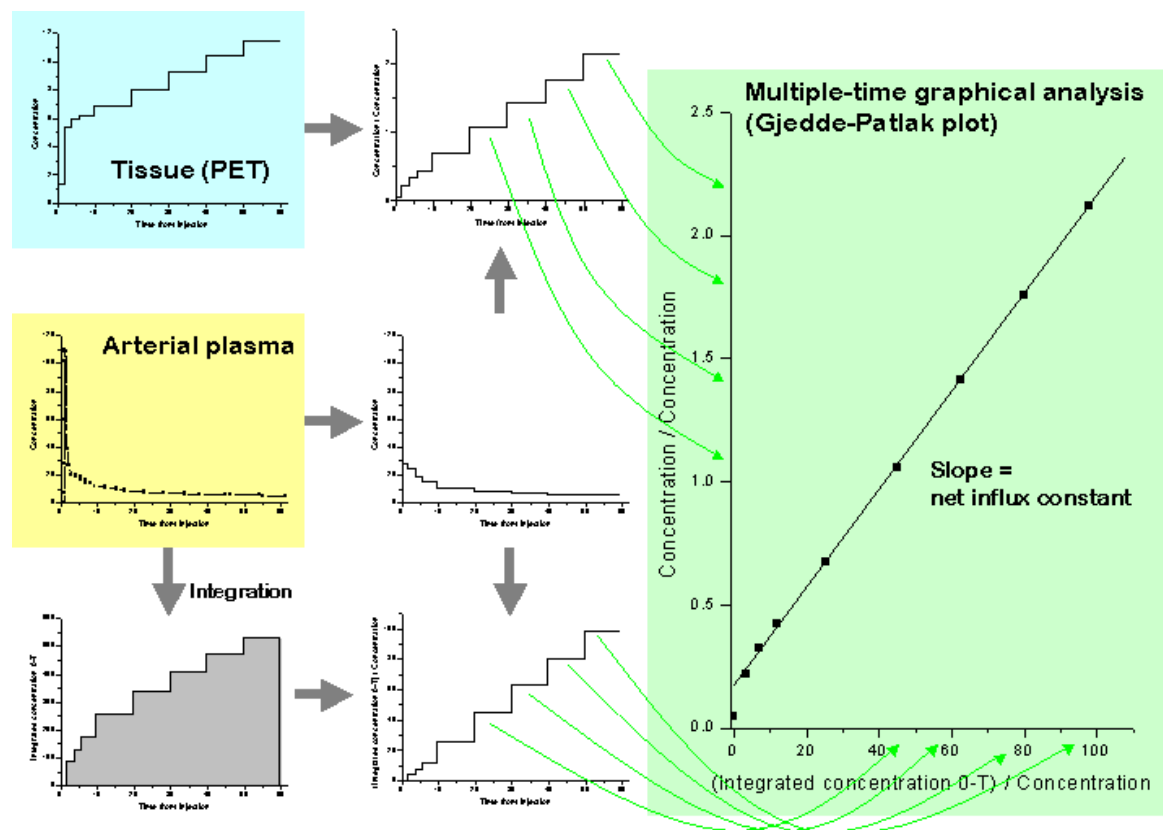
Determination of the value of the LC requires either





# Linearization methods are very often used to calculate MRglc from [ $^{18}\text{F}$ ]FDG PET

1. Based on compartment models with *irreversible binding*
2. *Clearance* (the amount of accumulated tracer in relation to the amount of tracer that has been available in plasma) is measured at *equilibrium* as the slope of the plot



## Gjedde-Patlak plot

The solution to a two-tissue compartment model ( $k_4=0$ ) is:

$$C_T = \frac{K_1}{k_2 + k_3} \left( k_2 e^{-(k_2+k_3)t} + k_3 \right) \otimes C_P$$

This was rearranged by Gjedde and Patlak:

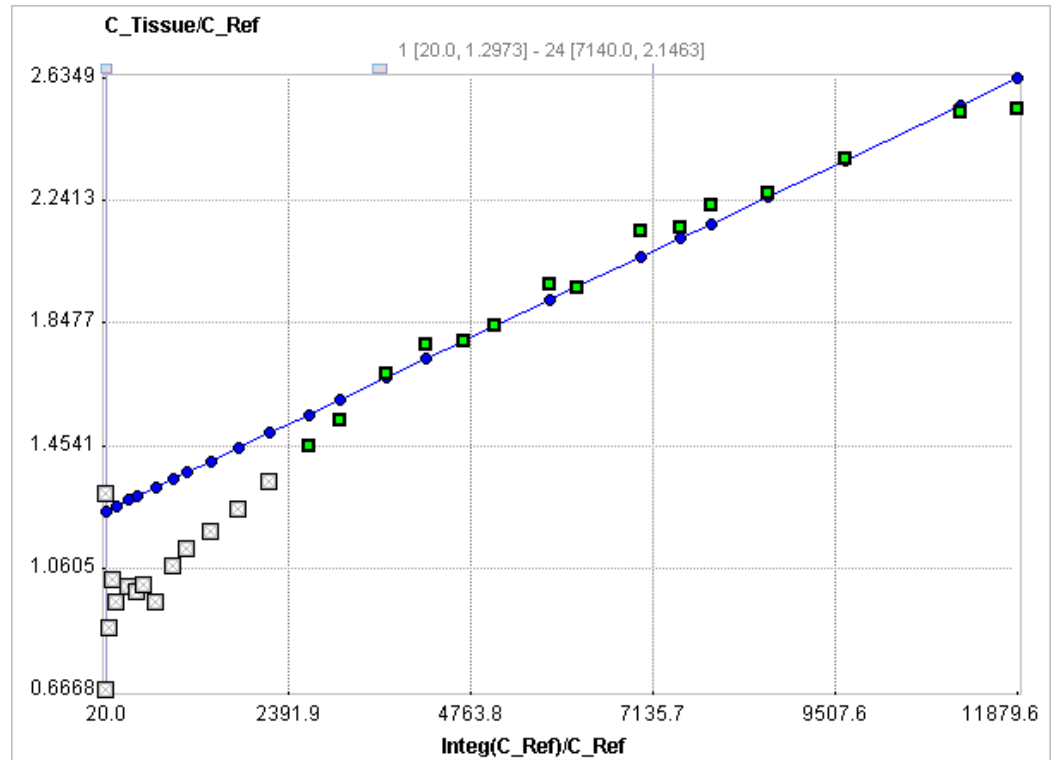
$$C_T = V_{ND} C_P + K_i \int_0^t C_P d\tau$$

Which after dividing by  $C_P$  is a straight line when  $t=t^*$ :

$$\frac{C_T}{C_P} = V_{ND} + K_i \frac{\int_0^t C_P d\tau}{C_P}$$

## Patlak plot

$$\frac{C_T}{C_P} = V_{ND} + K_i \frac{\int_0^t C_P d\tau}{C_P}$$



From the fitted line we therefore have:

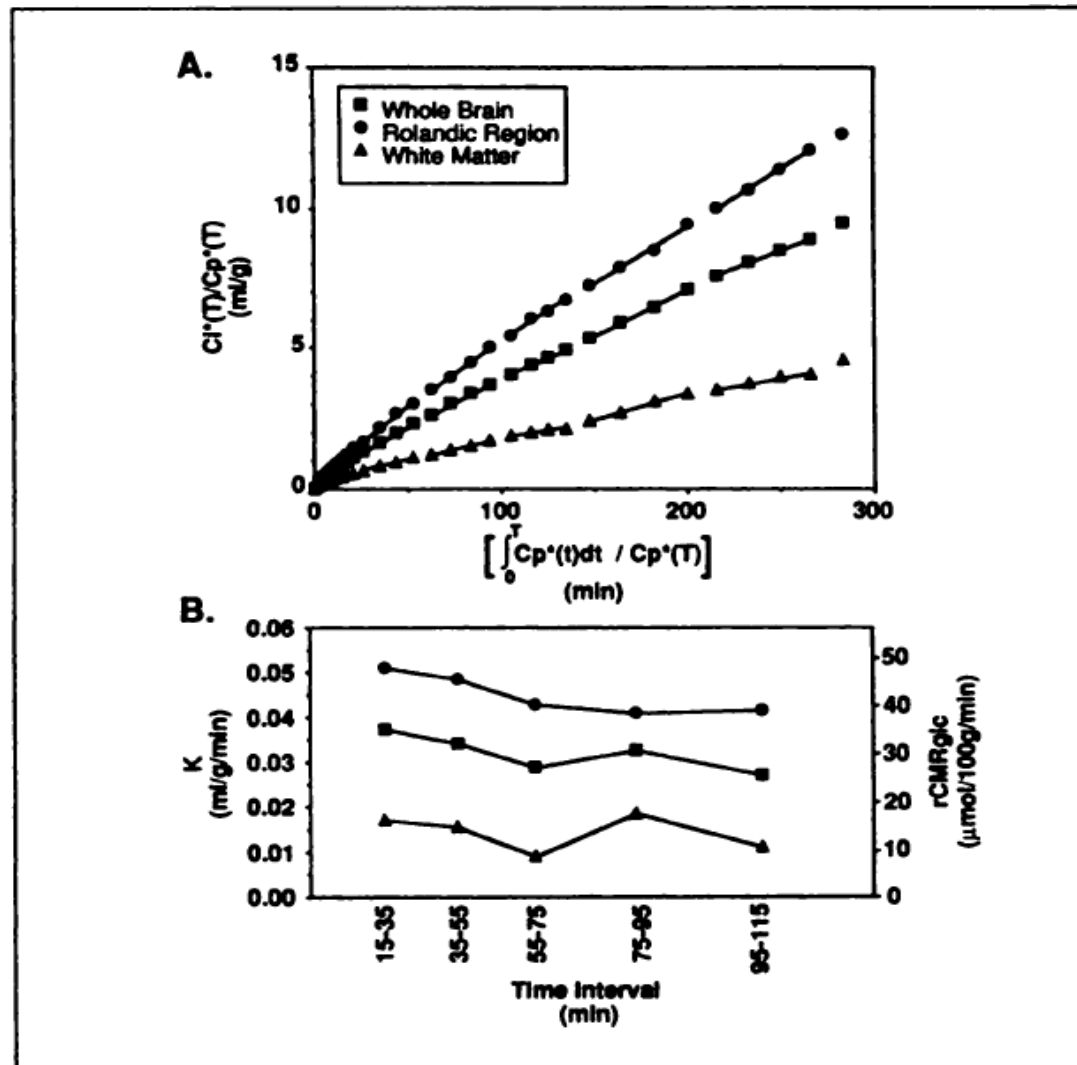
- The metabolic rate  $K_i = \frac{K_1 k_3}{k_2 + k_3}$  is the slope
- The distribution volume  $V_{ND} = \frac{K_1 k_2}{(k_2 + k_3)^2}$  is the intercept

## Graphical Linearization (Gjedde-Patlak Plot)

$K_i$  varies with segment  
used for determining the  
slope

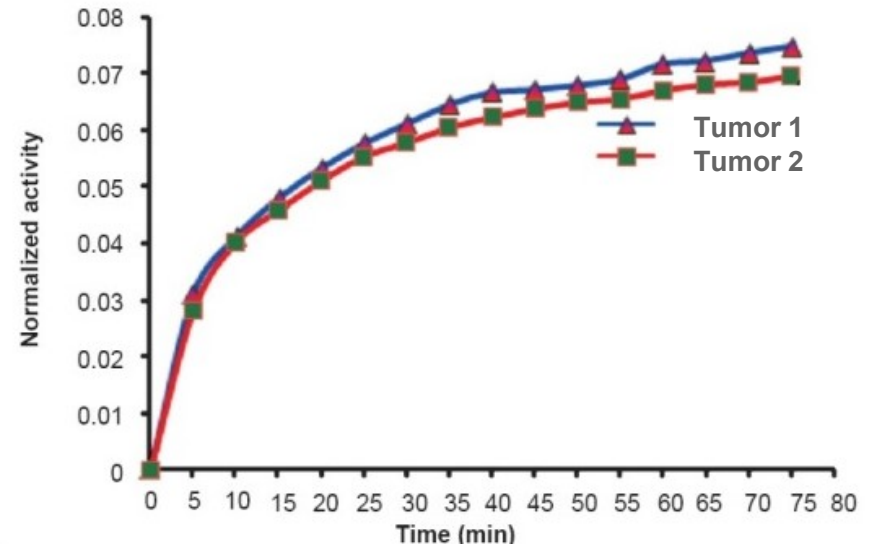
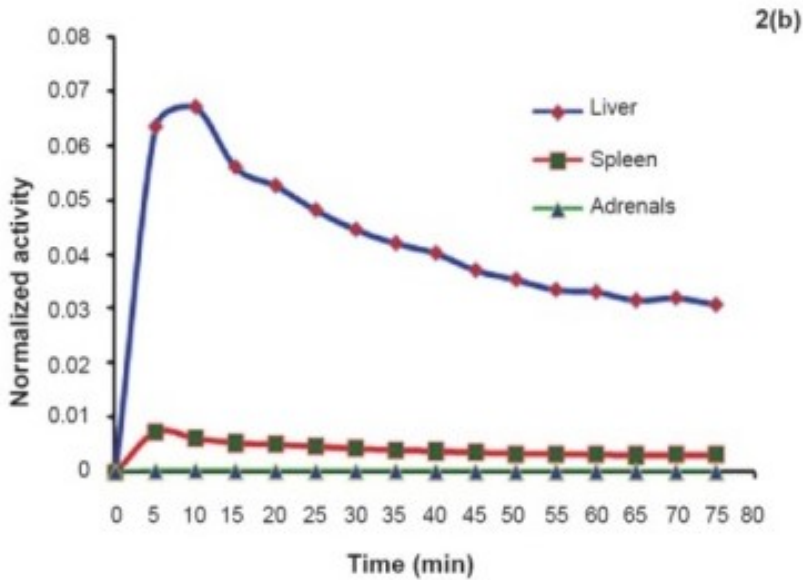
- why?

$k_4^* > \text{zero}$   
= tracer escapes from  
the brain, not true  
irreversible binding



**FIGURE 5.** "Patlak plots" of data obtained during scanning from 0 to 120 min following a pulse of  $[^{18}\text{F}]\text{FDG}$  for the whole brain, one gray matter structure and one white structure in a representative subject. (A) The graph shows five 20-min discrete linear segments for each of the three ROIs. Each segment was fitted to four consecutive points, starting and ending, respectively,

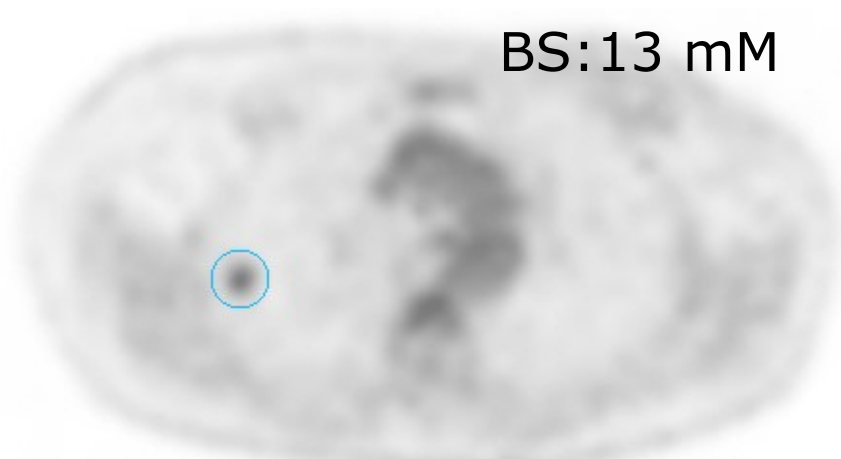
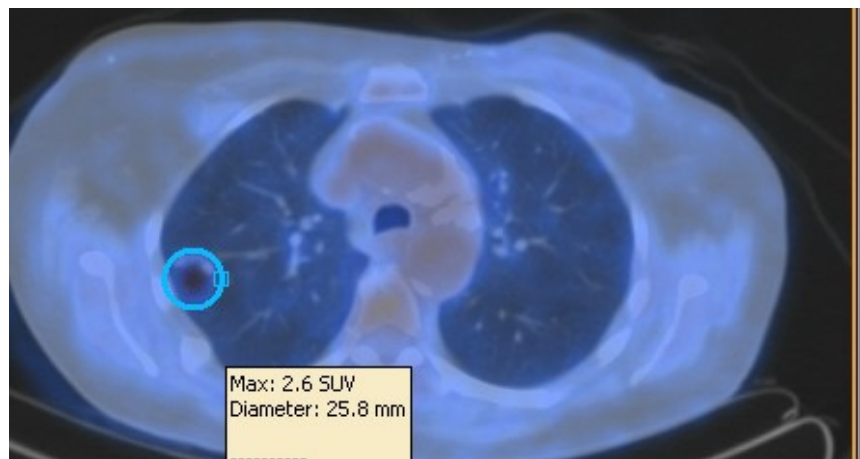
# [<sup>18</sup>F]FDG PET



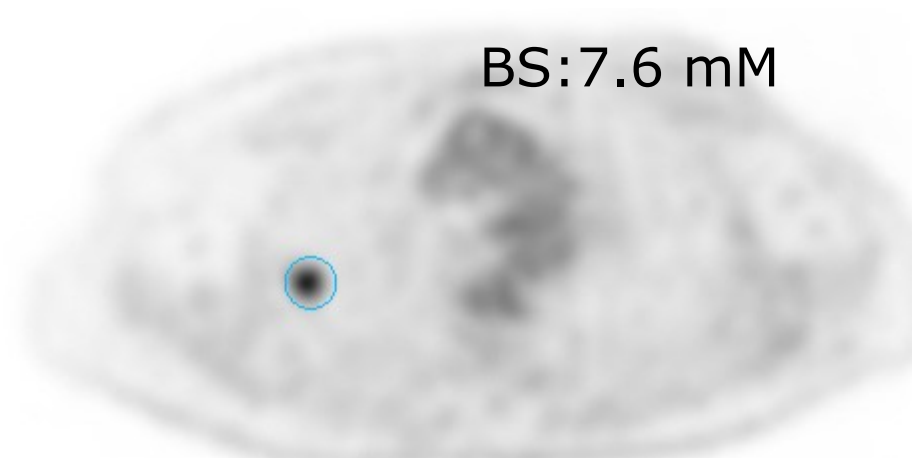
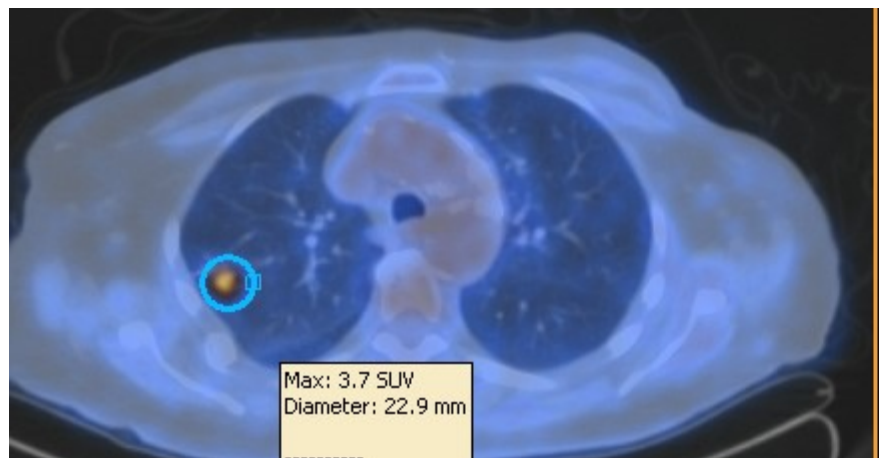
Q1: What is the difference between the liver curve on the left and the tumor curves on the right? What is the physiological difference?

Q2: Is FDG a reversible or irreversible tracer?

## FDG PET



What is the difference between the upper scan and the lower scan that was repeated a few days later?



## Blood glucose level


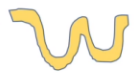
- High blood glucose levels (fasting? Diabetes?) interfere with FDG uptake
- When serum glucose  $> 8\text{mM}$ 
  - SUV in tumor drops from 5.1 to 2.8,  $p < 0.02$
  - SUV in skeletal muscles increase
- $K_i$  can decrease 25% with higher serum glucose
- Infusing insulin increase the translocation of GLUT 4 shunting FDG to organs with a high density of receptors (skeletal and cardiac muscles)
- Metformin strongly increase the SUV of the small and large intestines

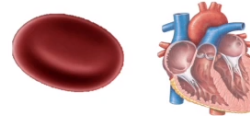


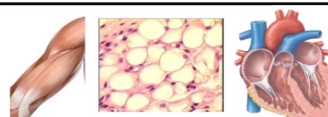
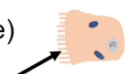



# Glucose transporters

Glucose is hydrophilic and need a transporter

## Sodium-Dependent Glucose Transporters

SGLT1	<ul style="list-style-type: none"> <li>• Enterocytes of Intestinal Epithelium (Luminal side)</li> </ul> 	<ul style="list-style-type: none"> <li>• Insulin-Independent</li> <li>• ATP- and Na-dependent</li> <li>• <i>Glucose Absorption</i></li> </ul>
SGLT2	<ul style="list-style-type: none"> <li>• Proximal tubule of nephron (Kidney)</li> </ul> 	<ul style="list-style-type: none"> <li>• Insulin-Independent</li> <li>• ATP- and Na-dependent</li> <li>• <i>Glucose Retention</i></li> </ul>

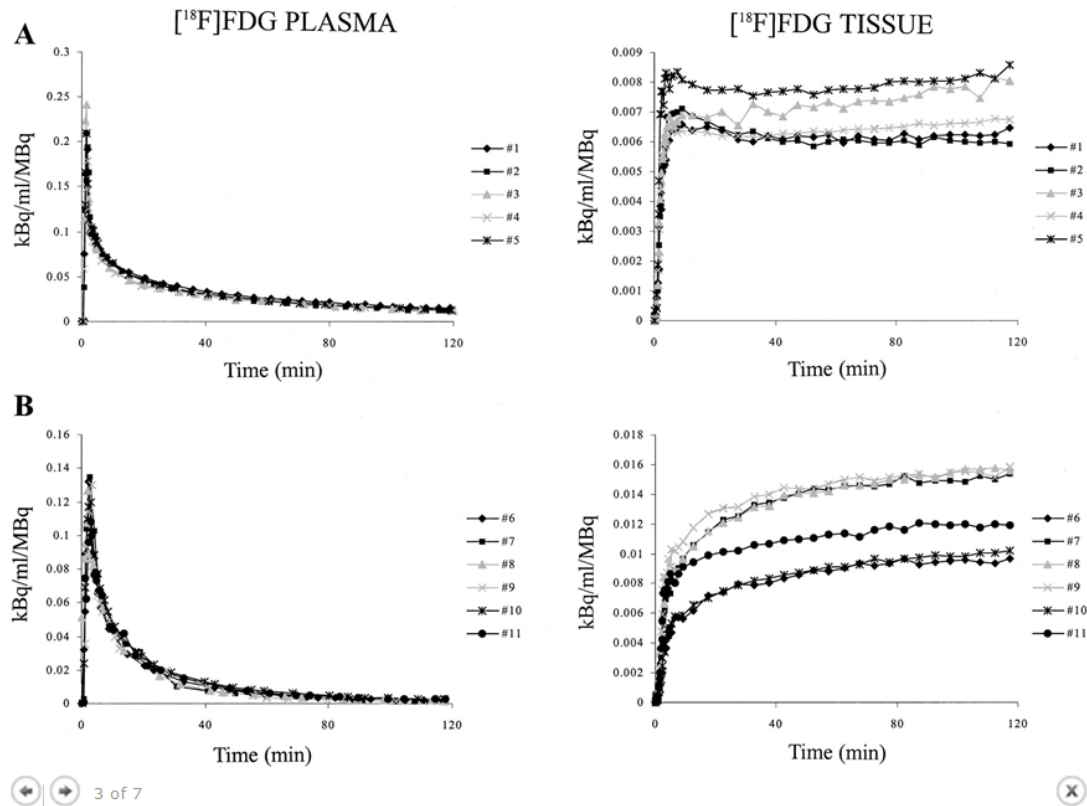
GLUT1	<ul style="list-style-type: none"> <li>• Blood</li> <li>• Blood-Brain Barrier</li> <li>• Heart (lesser extent)</li> </ul> 	<ul style="list-style-type: none"> <li>• Insulin-Independent</li> </ul>
GLUT2	<ul style="list-style-type: none"> <li>• Liver</li> <li>• Pancreas</li> <li>• Small Intestine</li> </ul> 	<ul style="list-style-type: none"> <li>• Insulin-Independent</li> <li>• High <math>K_m</math></li> <li>• Low Affinity</li> </ul>
GLUT3	<ul style="list-style-type: none"> <li>• Brain</li> <li>• Neurons</li> <li>• Sperm</li> </ul> 	<ul style="list-style-type: none"> <li>• Insulin-Independent</li> <li>• Low <math>K_m</math></li> <li>• High Affinity</li> </ul>
GLUT4	<ul style="list-style-type: none"> <li>• Skeletal Muscle</li> <li>• Adipose Tissue</li> <li>• Heart</li> </ul> 	<ul style="list-style-type: none"> <li>• <b>Insulin-Dependent***</b></li> <li>• Moderate <math>K_m</math></li> <li>• Moderate Affinity</li> </ul>
GLUT5	<ul style="list-style-type: none"> <li>• Enterocyte of Intestinal Epithelium (Luminal Side)</li> </ul> 	<ul style="list-style-type: none"> <li>• Insulin-Independent</li> <li>• <i>Fructose Transporter</i></li> </ul> 

[ $^{18}\text{F}$ ]FDG is not a good substrate for SGLT

Insulin level should be low to avoid GLUT4 that transport FDG into the muscles -> fasting!



## Tissue activity curves



Individual  $[^{18}\text{F}]\text{FDG}$  plasma and tissue time-activity (normalized to dose) curves in basal state (A, subjects 1–5) and during insulin stimulation (B, subjects 6–11).

Bertoldo et al. 2001 Am J Physiol Endocrinol Metab 281: E524-36

Fasting

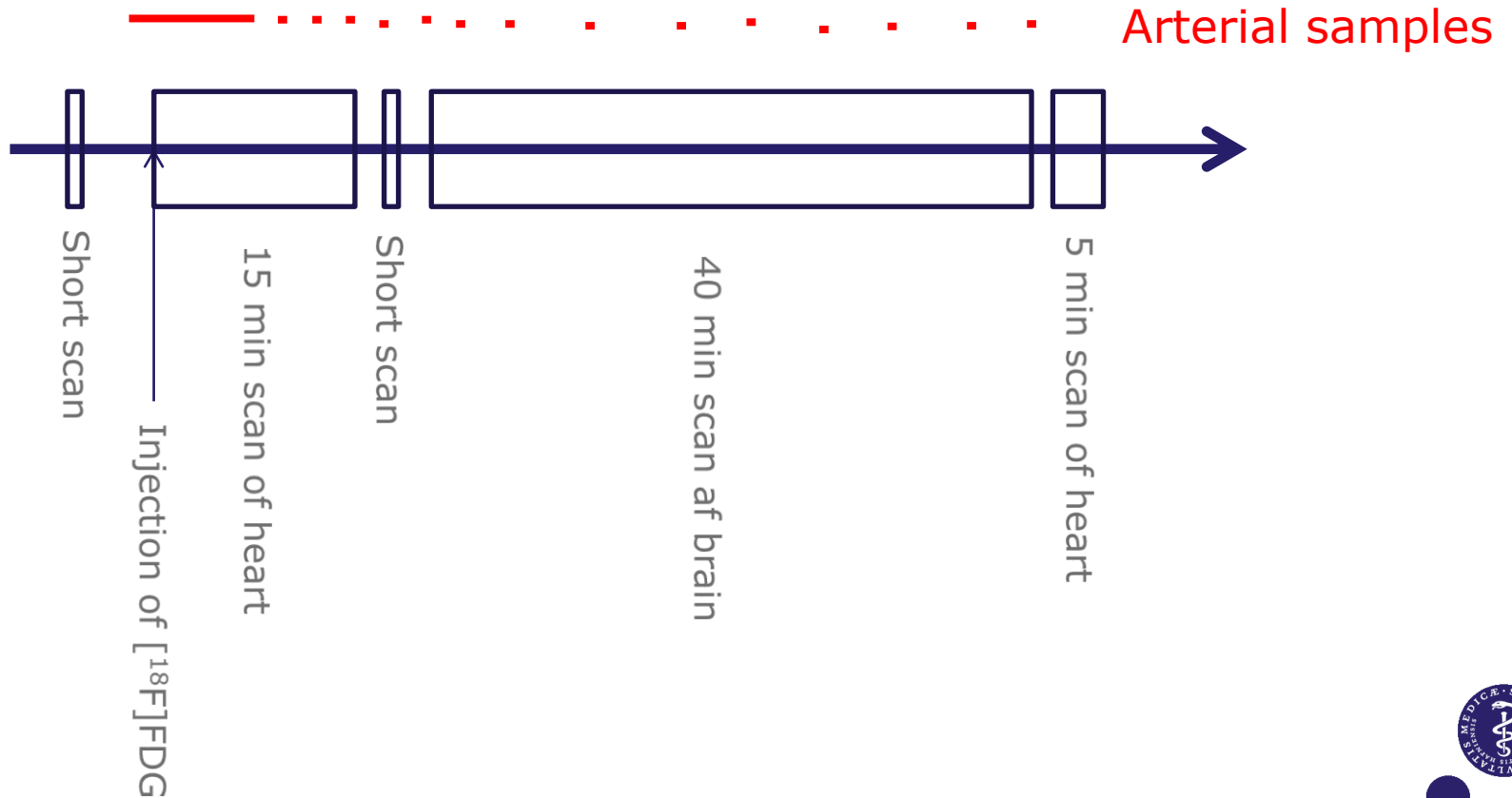
Insulin  
stimulation

# What happens during insulin stimulation?



# How to avoid arterial cannulation for rCMglc measurements

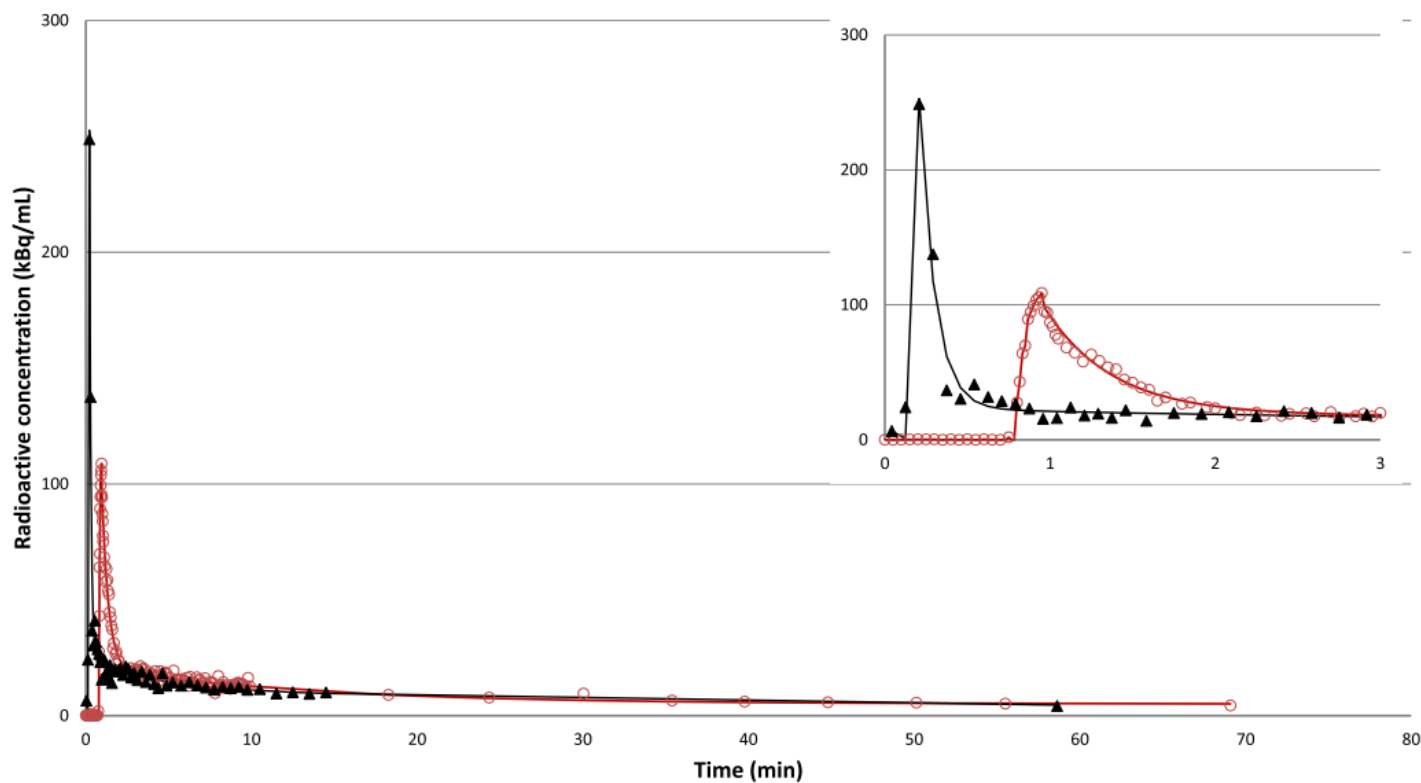
Scan procedure



# How to avoid arterial cannulation for rCMglc measurements

A.C. Henriksen, M.N. Lonsdale, D. Fuglø et al.

NeuroImage 253 (2022) 119079

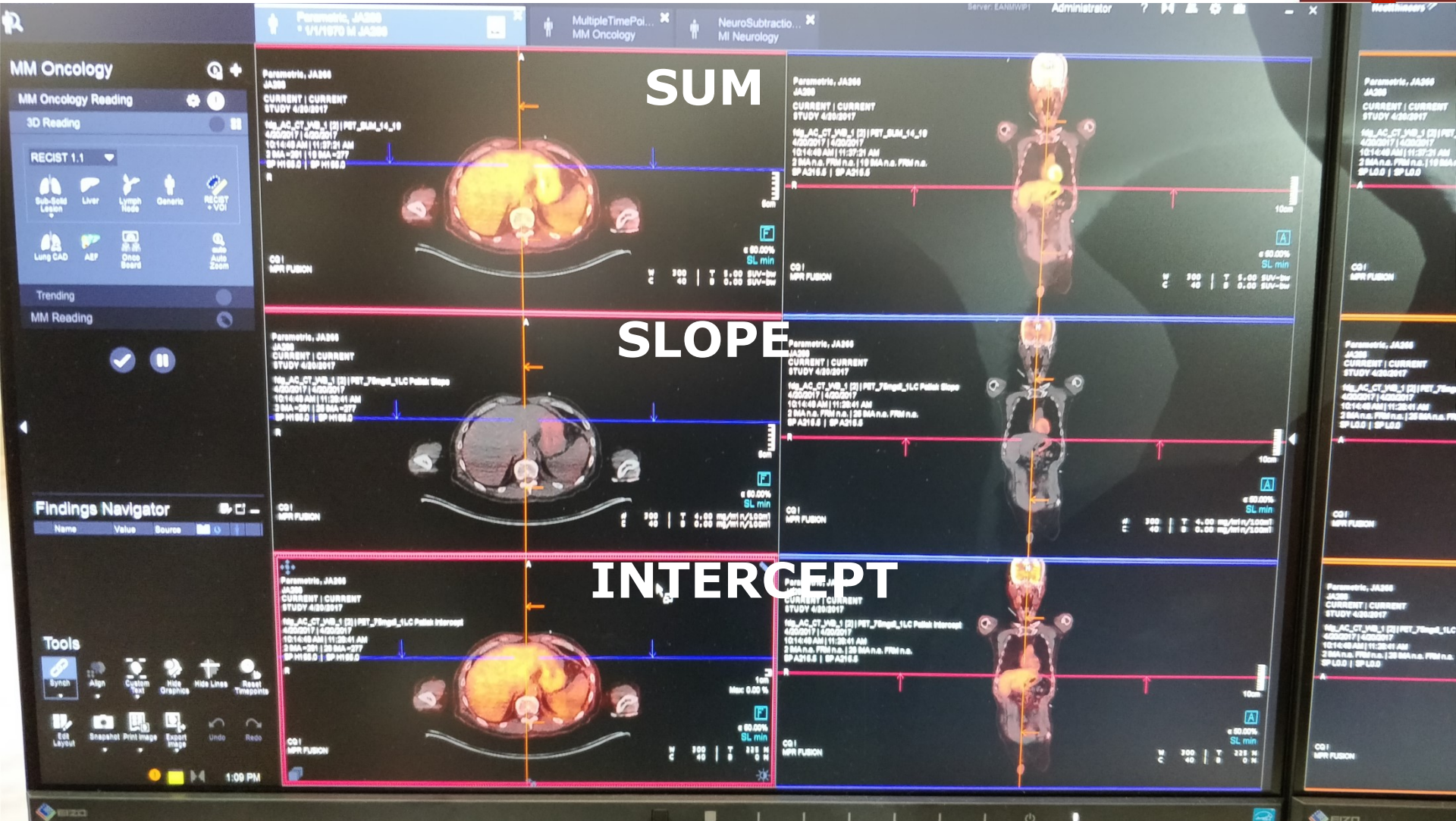


**Fig. 1.** Plot of the fitted arterial (AIF, red hollow circles) and image derived (IDIF, filled triangles) inputfunction. Top right the first 3 min. Note the earlier and narrower IDIF peak.





# Scanners with build-in Gjedde-Patlak plot reconstruction



Siemens, Knoxville, USA

## Methods to avoid the arterial cannulation

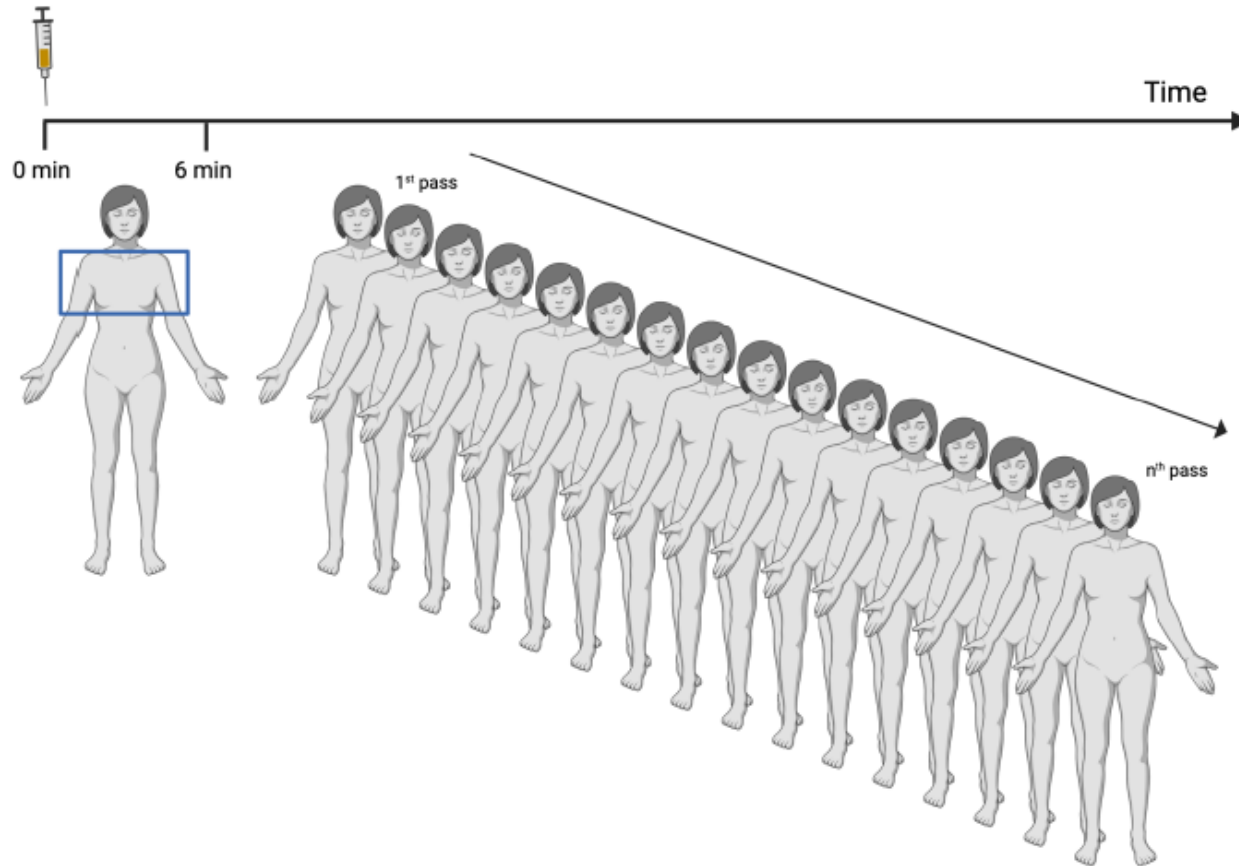
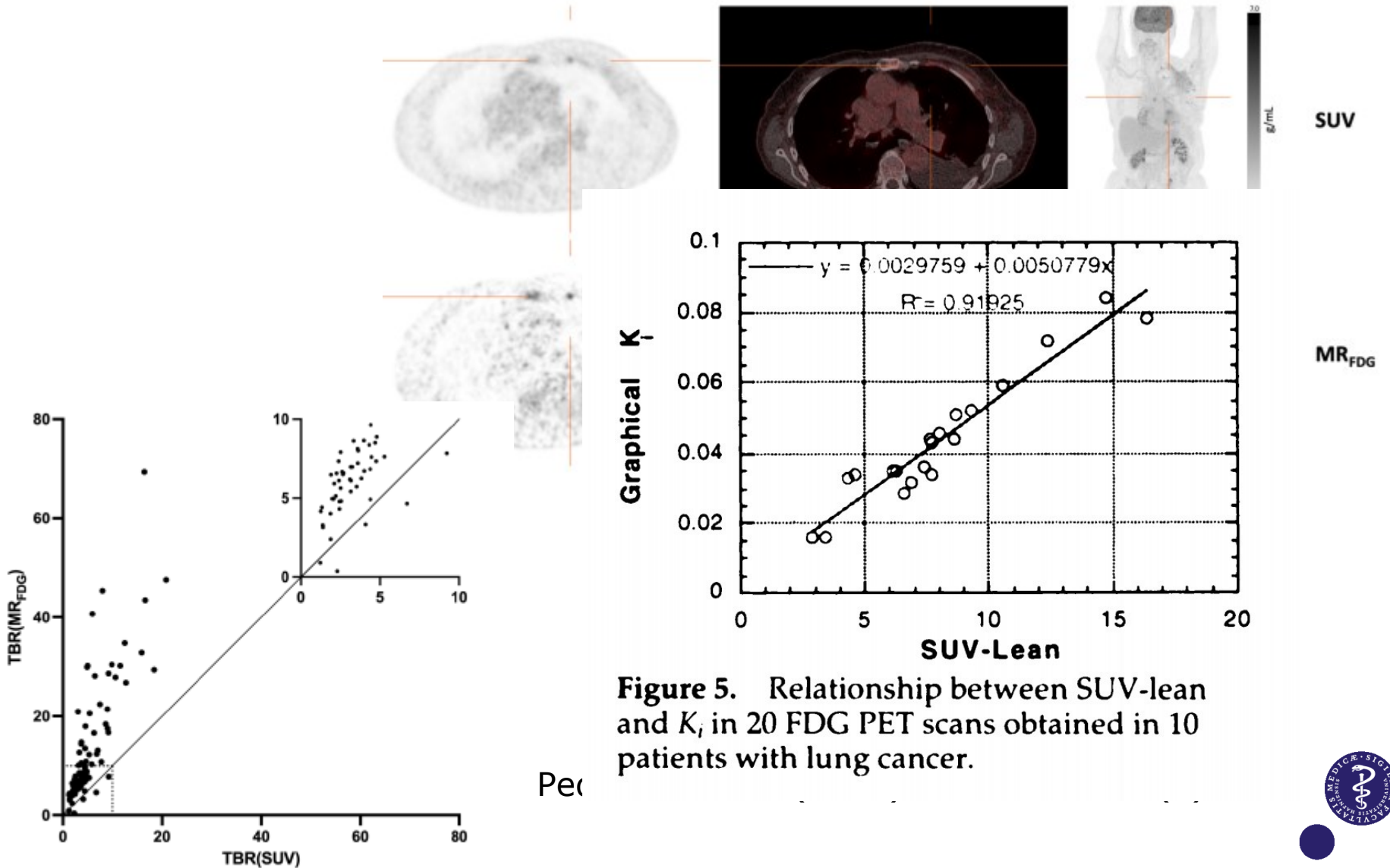


Figure 2: Example of a dynamic whole-body (D-WB) PET acquisition protocol including an initial 6-minute dynamic scan over the chest region, followed by a D-WB scan with multiple continuous bed motion passes

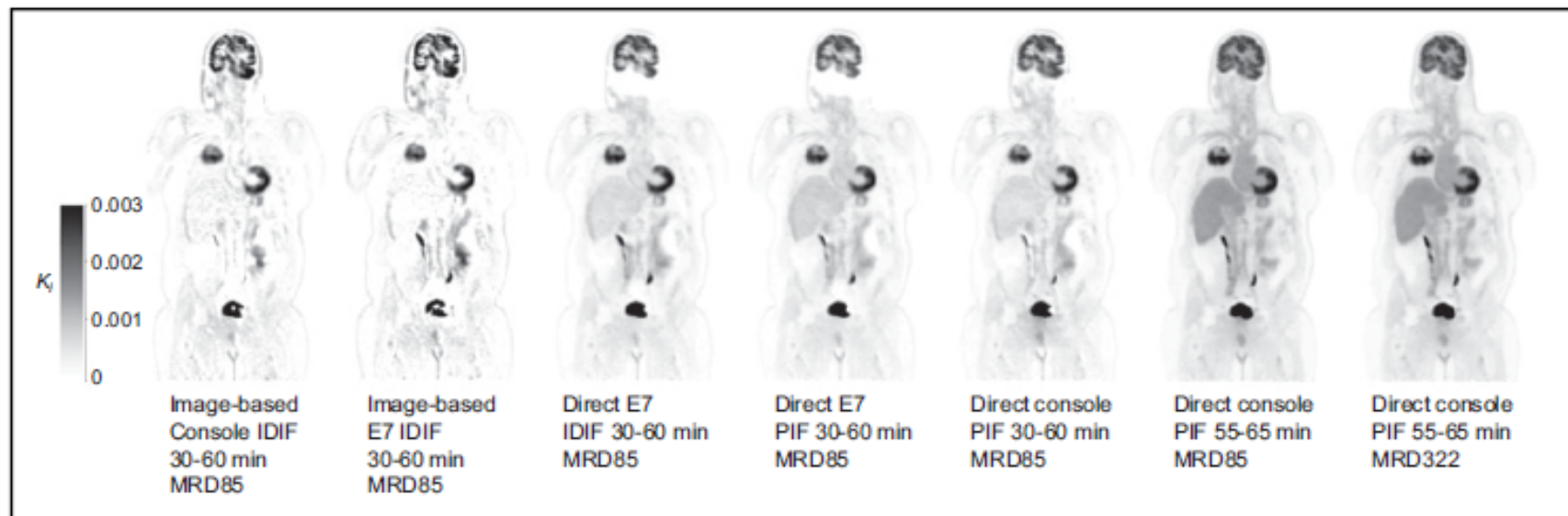
# How to avoid arterial cannulation for rCMglc measurements



**Figure 5.** Relationship between SUV-lean and  $K_i$  in 20 FDG PET scans obtained in 10 patients with lung cancer.

Pec

# Whole-Body [ $^{18}\text{F}$ ]FDG Patlak Imaging Using LAFOV PET



**FIGURE 1.** Example coronal parametric  $K_i$  images of 65-y-old man with non-small cell lung cancer. Images were obtained with different approaches using IDIF or scaled PIF at different intervals after injection.